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A New Approach to Image Denoising by Patch-Based Algorithm

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Abstract: Different types of denoising methods are existed in databases. But every method has its own uniqueness. We propose a new method that is adaptive patch based system for image denoising. The approach depends on a pointwise selection of narrow image patches of precise size in the variable neighborhood of each pixel. Our contribution is to engage in each pixel the weighted sum of data points not outside an adaptive neighborhood, in a sense that it balances the efficiency of estimation and the stochastic error, at each contiguous position. In this paper introducing spatial adaptivity, we prolong the work that can be designed as a development of bilateral filtering to image patches. This method is tested by using AWGN and images are taken from databases with different resolutions. The performance of the denoising system is computed in terms of PSNR by taking different noise levels.

Keywords: Image denoising; bilateral filtering; mean-squared-error (MSE) estimator; PSNR; Patch based method.

I. INTRODUCTION

In recent years, images captured by present-day cameras Where Δ_i is the window centered at pixel x_i , Y_i is the are habitually corrupted by noise [3]. With increasing pixel resolution but more or less the same aperture size. noise elimination has turn into more relevant. While advances in optics and hardware try to mollify such abominable effects, software-based denoising approaches are more familiar as they are normally device independent and extensively suitable. In the last decade, many such methods have been recommended, lead to extensive enhancement in denoising performance. In [1] and [2], we studied the dispute from an estimation theory aspect to compute the fundamental limits of denoising. The insights gained from that study are applied to promote a hypothetically sound denoising method in this paper. Most of the more competent regularization methods depend on energy functional minimization therefore they are designed to deliberately account for the image geometry, involving the compromise of global weights that weigh the contribution of prior gracefulness terms and a fidelity term [13]. Thus, associated partial differential equations (PDEs) and variationally methods have demonstrated intense results to take up the dispute of edge-preserving smoothing [9], [10], [11], [23], [28]. For reasons of performance and robustness in image processing, other smoothing algorithms cumulative information over a neighborhood of fixed size, based on two primitive criteria: a spatial criterion in order that filtering must be local and a brightness criterion to counterbalance choose only points that are identical in some sense. In view about generic approach, a typical filter is the sigma filter [32]. The well-known nonlinear Gaussian filter [25] defined as

$$\hat{u}(x_i) = \frac{\sum_{x_j \in \Delta_i} L_g(Y_i - Y_j)Y_j}{\sum_{x_j \in \Delta_i} L_g(Y_i - Y_j)}$$
(1)

observation at x_i ,

$$L_g(z) = \exp\left(\frac{-z^2}{2g^2}\right) \tag{2}$$

and g is a smoothing parameter to be determined and depends on the signal-to-noise ratio (SNR). Finally, if we substitute a Gaussian window to the hard-curved window almost the current position, we get variants of the bilateral filtering.

$$\hat{u}(x_i) = \frac{\sum_{x_j \in \Delta_i} L_g(Y_i - Y_j) K_h(x_i - x_j) Y_j}{\sum_{x_j \in \Delta_i} L_g(Y_i - Y_j) K_h(x_i - x_j)}$$
(3)

where $K_h(x_i - x_i)$ and $L_p(Y_i - Y_i)$ are rescaled versions of nonnegative kernel functions K and L. In specific, Mrazek brought out the multiple of structural similarities between the iterated bilateral filter.

$$\hat{u}_{n+1}(x_i) = \frac{\sum_{x_j \in \Delta_i} L_g(\hat{u}_n(x_i) - \hat{u}_n(x_j)) K_h(x_i - x_j) \hat{u}_n(x_j)}{\sum_{x_j \in \Delta_i} L_g(\hat{u}_n(x_i) - \hat{u}_n(x_j)) K_h(x_i - x_j)}$$
(4)

and local M-smoother

$$\hat{u}_{n+1}(x_i) = \frac{\sum_{x_j \in \Delta_i} W_g(Y_j - \hat{u}_n(x_i)) K_h(x_i - x_j) Y_j}{\sum_{x_j \in \Delta_i} W_g(Y_j - \hat{u}_n(x_i)) K_h(x_i - x_j)}$$
(5)

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where
$$W_{g}(Y_{j} - \hat{u}_{n}(x_{i})) = \rho_{z}^{1}(Y_{j} - \hat{u}_{n}(x_{i}))$$
 and

 $\rho_z(Y_i - \hat{u}_n(x_i))$ is the error norm for M-estimators. It is proved that regional M-smoothing uses the initial image in the averaging procedure and determine the minimum of a local criterion considering that iterated bilateral filtering uses the evolving image and must stop subsequently a particular number of iterations in order to avoid a flat image [15]- [20].

To promote better image enhancement algorithms that can supervise structured noise, we need precise models for the many regularities and geometries seen in local patterns. In comparison, a distinct line of work consists then in modelling non-local pairwise interactions from training data [29] or a library of natural image patches [21], [27]. The data points with an identical patch to the central patch will have larger weights in the average as recently proposed by Buades [7], [8] who defined the purported non-local means filter as

$$\hat{u}(x_i) = \frac{\sum_{x_j \in \Delta_i} L_g(Y_i - Y_j) K_h(x_i - x_j) Y_j}{\sum_{x_j \in \Delta_i} L_g(Y_i - Y_j) K_h(x_i - x_j)}$$
(6)

Where Y_i denotes a vector of pixel values taken in the neighborhood of a point x_i . In (5), the similarity between two points x_i and x_j is based on the Euclidean distance $\left\|Y_{i}-Y_{j}\right\|^{2}$ between two vectorized image patches (see also [58]). It stands observing that, if the size of the patch is reduced to one pixel, the non-local means filter, also controlled by a small number of smoothing parameters and, is closely equivalent to (2). As in [30], [31], [36], we also use narrow image patches (e.g., 7x7 or 9x9 patches) to enumerate the particular weights therefore they allow capture regional geometric patterns and texels seen in image s. Moreover, we adaptively determine a window (neighborhood) that probably large to balance the accuracy of approximation and the stochastic error, at each spatial position [34]. This transformation method is a moderately change-point detection procedure introduced by Lepskii [33]. The recommended procedure shares some common points with the contemporary non-local means algorithm [17], other patch -based methods [15], [18], [29] and the DUDE algorithm. In [16], the authors design a two-pass approach and substitute the most frequent patch /symbol seen in a local window to the current perverted patch /symbol.

The paper is organized as follows. In Section II, tells about problem statement and introduce the image modeling and some notations. In Section III, we formulate the adaptive Section IV, we demonstrate the ability of the method where $\hat{V}_{,n-1}$ is $p^2 \times p^2$ diagonal matrix of the form (the weights and patch based algorithm for image denoising. In to restore artificially corrupted images with additive white symbol "." is used to denote a spatial position)

Gaussian noise (WGN) with different sigma values. Conclusions are presented in Section V.

II. PROBLEM STATEMENT

In comparison to exemplar-based approaches for image modeling [14], [19], we propose an unsupervised method that uses no library of image patches and no computational intensive training algorithms [23]. Our adaptive smoothing introduces the joint spatial range domain as the non-local means filter [13] but has a more dominant adaptation to the local structure of the data therefore the size of windows and control parameters are predicted from local image statistics as follows.

Consider the following basic image model:

$$Y_i = u(x_i) + \varepsilon_i, \quad i = 1, 2, 3..., |G|$$
 (7)

where $x_i \in G \subset \mathbb{R}^d$, $d \ge 2$ represents the spatial coordinates of the discrete image domain of |G| pixels, and $Y_i \in R_+$ is the observed intensity at location x_i . For clarity, an image patch u_i is cast as a fixed size square window of $p \times p$ pixels centered at x_i . In what follows,

 u_i will stand for inadequately a patch or a vector of p^2 elements where the pixels are concatenated along a fixed lexicographic ordering. As with all patch -based techniques, the size of image patches must be described in advance [31], [32], [35]. Traditionally, the size of the image patch is a parameter-free that specifies how stochastic the user believes the image to be. However, we will see that a patch size of 7x7 or 9x9 pixels manage take care of the local geometries and textures in the image while removing unwanted distortions. Finally, the suggested method requires no training step and may be then treated as unsupervised.

III. IMPLEMENTATION OF ADAPTIVE PATCH BASED SYSTEM

A. Adaptive Weights

In order to compute the similarity between patches $\hat{u}_{i,n} = \sum_{x_j \in \Delta_{i,n}} \pi_{i \sim j,n} Y_j$ and $\hat{u}_{j,n}$, a distance must be considered. In [7], [15], [18] several authors showed that the L_2 distance $\left\|\hat{u}_{i,n} - \hat{u}_{j,n}\right\|^2$ is a reliable measure to compare image patches. To make a decision, we have rather used the following normalized distance

$$dist(\hat{u}_{i,n-1},\hat{u}_{j,n-1}) = \frac{1}{2} \begin{bmatrix} (\hat{u}_{i,n-1} - \hat{u}_{j,n-1})^T \hat{V}_{i,n-1}^{-1} (\hat{u}_{i,n-1} - \hat{u}_{j,n-1}) + \\ (\hat{u}_{j,n-1} - \hat{u}_{i,n-1})^T \hat{V}_{j,n-1}^{-1} (\hat{u}_{j,n-1} - \hat{u}_{i,n-1}) \end{bmatrix}$$
(8)



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$$\hat{V}_{,n-1} = \begin{pmatrix} \left(\hat{v}_{,n-1}^{(1)} \right)^2 & 0 & \cdots & 0 \\ 0 & \left(\hat{v}_{,n-1}^{(2)} \right)^2 & \cdots & 0 \\ \vdots & \vdots & \vdots & \vdots \\ 0 & \cdots & 0 & \left(\hat{v}_{,n-1}^{(p^2)} \right)^2 \end{pmatrix}$$
(9)

where $\hat{v}_{l,n-1}^{(l)}$, $l=1,2,\ldots,p^2$, is the local standard deviation of the estimator $\hat{v}_{.,n-1}^{(l)}$, and the index *l* is used to $\begin{array}{c} \text{Our results were measured by the peak signal-to-noise ratio (PSNR) in decibels (dB) defined as} \end{array}$ denote a spatial position in an image patch $\hat{u}_{i,n-1} = \left(\hat{u}_{i,n-1}^{(1)}, \dots, \hat{u}_{i,n-1}^{(l)}, \dots, \hat{u}_{i,n-1}^{(p^2)}\right)^T$

Henceforth, we introduce the following commonly used where u_0 is the noise-free original image. weight function

$$\pi_{i \sim j,n} = \frac{K\left(\lambda_{\alpha}^{-1} dist\left(\hat{u}_{i,n-1}, \hat{u}_{j,n-1}\right)\right)}{\sum_{x_{j} \in \Delta_{i,n}} K\left(\lambda_{\alpha}^{-1} dist\left(\hat{u}_{i,n-1}, \hat{u}_{j,n-1}\right)\right)}$$
(10)

 $K\left(\lambda_{\alpha}^{-1}dist\left(\hat{u}_{i,n-1},\hat{u}_{j,n-1}\right)\right)$ denoting a monotone with decreasing function, e.g., a kernel $K(z) = \exp(-z/2)$. Due to the fast decay of the exponential kernel, large distances between predicted patches provoke nearly zero weights. Note that the use of weights enables to relieve the structural hypothesis that the neighborhood is practically modeled by a square window.

B. Patch based image denoising algorithm

- i. Let $\{p, \alpha, \tilde{n}, N_{\Lambda}\}$ be the parameters
- ii. Initialization: Compute $\hat{\sigma}^2$ and $\{\hat{u}_{i,0}, \hat{u}_{i,0}^2\}$ for each

$$x_i \in G$$
 and set $n = 1$

- iii. Repeat
- for each $x_i \in G$ •

-Compute

$$\pi_{i \sim j,n} = \frac{K\left(\lambda_{\alpha}^{-1} dist\left(\hat{u}_{i,n-1}, \hat{u}_{j,n-1}\right)\right)}{\sum_{x_{j} \in \Delta_{i,n}} K\left(\lambda_{\alpha}^{-1} dist\left(\hat{u}_{i,n-1}, \hat{u}_{j,n-1}\right)\right)}$$
$$\hat{u}_{i,n} = \sum_{x_{j} \in \Delta_{i,n}} \pi_{i \sim j,n} Y_{j}$$
$$\hat{v}_{i,n}^{2} = \hat{\sigma}^{2} \sum_{x_{j} \in \Delta_{i,n}} \left[\pi_{i \sim j,n}\right]^{2}$$

-Choose the window as

$$\hat{\Delta}(x_i) = \arg \max_{\Delta_{i,n\in\mathbb{N}_{\Delta}}} \left\{ \begin{vmatrix} \Delta_{i,n} | \vdots | \hat{u}_{i,n} - \hat{u}_{i,n'} \\ \leq \tilde{n} \hat{u}_{i,n'}, \end{vmatrix} \text{ for all } 1 \leq n' < n \right\}$$

If this rule is violated at iteration *n* , we do not accept $\hat{u}_{i,n}$

and keep the estimate
$$\hat{u}_{i,n-1}$$
 as the final estimate x_i , i.e.
 $\hat{u}(x_i) = \hat{u}_{i,n-1}$ and $\hat{n}(x_i) = n-1$. This estimate is
unchanged at the next iterations and x_i is frozen.
• Increment n
iv. while $n \le N_{\Delta}$

$$PSNR = 10 \log_{10} \left(\frac{255 \times 255}{MSE} \right), MSE = \frac{\sum_{x_i \in G} \left(u_0(x_i) - \hat{u}(x_i) \right)^2}{G}$$



Fig. 1. Illustration of LENA image at sigma=2



(a) Original Image



(c) Difference Image



(b) Noisy Image



(d) Denoised Image

Fig.2. Illustration of LENA image at sigma=4



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(a) Original Image



(c) Difference Image

Fig.3. Illustration of LENA image at sigma=7



(a) Original Image



(c) Difference Image

Fig. 4. Illustration of LENA image at sigma=9



(a) Original Image



(c) Difference Image

Fig.5. Illustration of LENA image at sigma=15



(b) Noisy Image



(d) Denoised Image



(b) Noisy Image







(b) Noisy Image



(d) Denoised Image



(a) Original Image



(c) Difference Image



(b) Noisy Image



(d) Denoised Image

(b) Noisy Image

Fig.6. Illustration of LENA image at sigma=25



(a) Original Image



(c) Difference Image

Fig.7. Illustration of LENA image at sigma=45



(a) Original Image



(c) Difference Image





(b) Noisy Image



(d) Denoised Image

Fig.8. Illustration of LENA image at sigma=70



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(b) PSNR at sigma=4



(c) PSNR at sigma=7





Fig. 9. Different PSNR values of LENA image at different noise levels



(a) PSNR values of LENA at different sigma value



(b) Histogram representation of LENA at different sigma values

Fig10 Comparison of LENA image at different noise levels



Fig.11. Histogram representation of PSNR versus sigma



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TABLE 1: DENOISING RESULTS OF LENA IMAGE BY TAKING DIFFERENT SIGMA VALUES

Iterati	Sigma=2	Sigma=4	Sigma=7	Sigma=9	Sigma=15	Sigma=25	Sigma=45	Sigma=70
ons	APBS	APBS	APBS	APBS	APBS	APBS	APBS	APBS
1	43.41	39.03	35.72	34.19	30.93	26.08	20.33	15.87
2	43.56	39.51	36.78	35.60	33.15	29.02	23.31	18.32
3	43.64	39.73	37.23	36.18	34.03	31.22	26.88	21.69
4	43.66	39.78	37.36	36.35	34.25	31.88	28.81	25.25
5	43.65	39.77	37.40	36.41	34.33	32.09	29.33	26.87
6	43.61	39.75	37.41	36.43	34.35	32.17	29.51	27.36
7	43.58	39.74	37.42	36.44	34.36	32.22	29.60	27.58
8	43.54	39.72	37.42	36.44	34.36	32.24	29.72	27.85

V. CONCLUSION

In this paper, the proposed method that is adaptive patchbased weights and variable window sizes are simultaneously used. An advantage of the method is that subjective parameters can be easily chosen and are comparably stable. The method allows denoise both piecewise-smooth and textured real images therefore they consist of adequate redundancy. Actually. the performance of our method is very close, and in some cases even surpasses, to that of the earlier published denoising methods. Also, we just discuss that the method can be easily correlate therefore at iteration, each pixel is processed independently. Here we have better results in terms of PSNR compared to other methods.

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